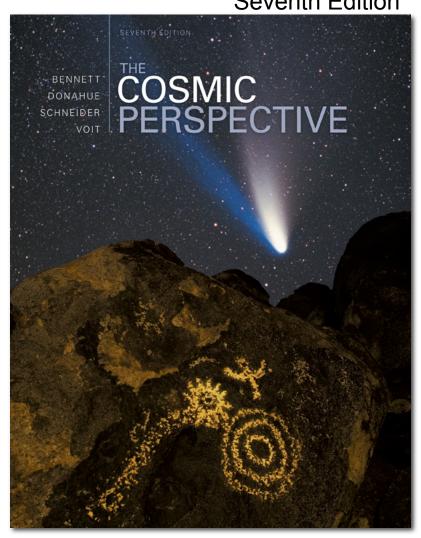
Chapter 15 Lecture

The Cosmic Perspective

Seventh Edition

Surveying the Stars

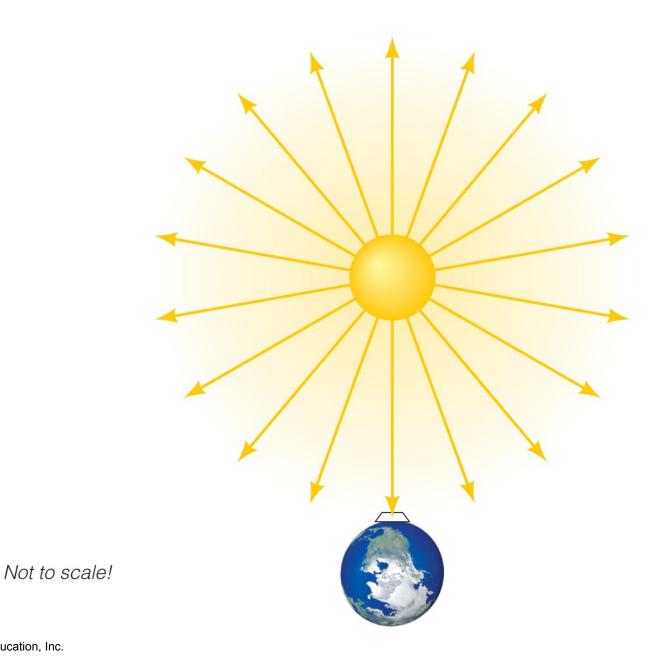


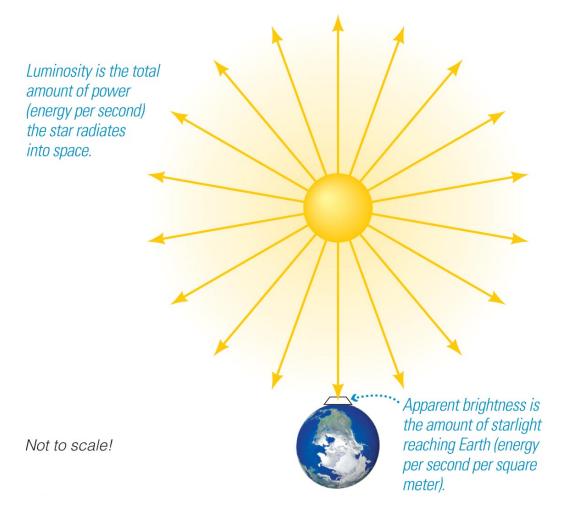
15.1 Properties of Stars

- Our goals for learning:
 - How do we measure stellar luminosities?
 - How do we measure stellar temperatures?
 - How do we measure stellar masses?



How do we measure stellar luminosities?



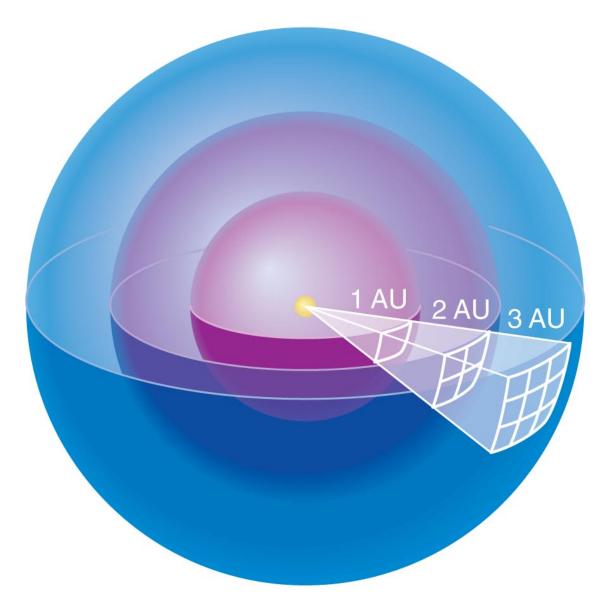


Luminosity:

 Amount of power a star radiates (energy per second = watts)

Apparent brightness:

 Amount of starlight that reaches Earth (energy per second per square meter)



 The amount of luminosity passing through each sphere is the same.

Area of sphere: 4π (radius)²

Divide luminosity by area to get brightness.

Inverse Square Law

 The relationship between apparent brightness and luminosity depends on distance:

Brightness =
$$\frac{\text{Luminosity}}{4\pi \text{ (distance)}^2}$$

• We can determine a star's luminosity if we can measure its distance and apparent brightness:

Luminosity =
$$4\pi$$
 (distance)² × (brightness)

UNITS:

```
apparant brightness (or flux) in J s<sup>-1</sup> m<sup>-2</sup> (W m<sup>-2</sup>) source luminosity in J s<sup>-1</sup>(W) distance between observer and source in meters
```

Thought Question

How would the apparent brightness of Alpha Centauri change if it were three times farther away?

- A. It would be only 1/3 as bright
- B. It would be only 1/6 as bright.
- C. It would be only 1/9 as bright.
- D. It would be three times brighter.

Thought Question

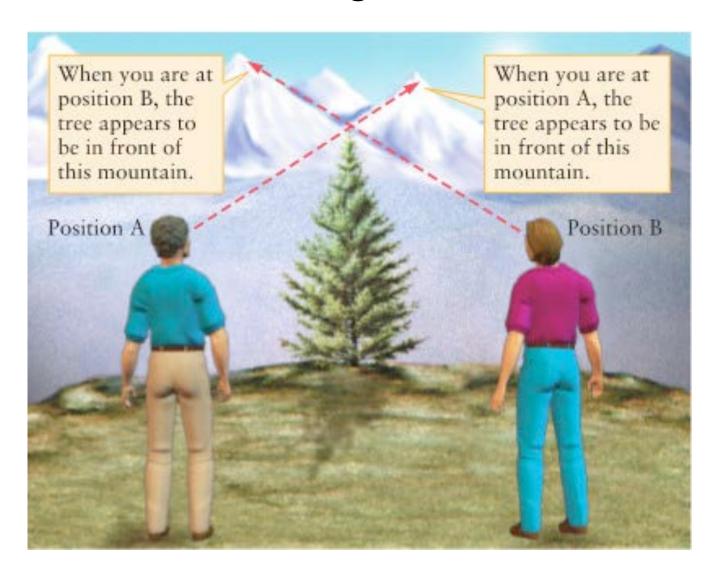
How would the apparent brightness of Alpha Centauri change if it were three times farther away?

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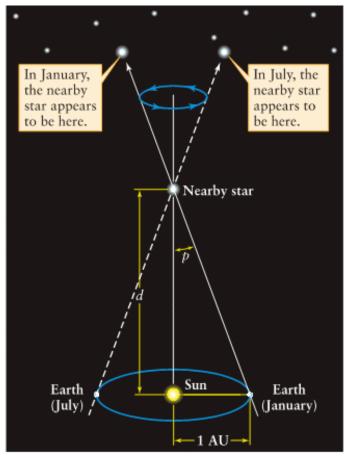


So how far away are these stars?

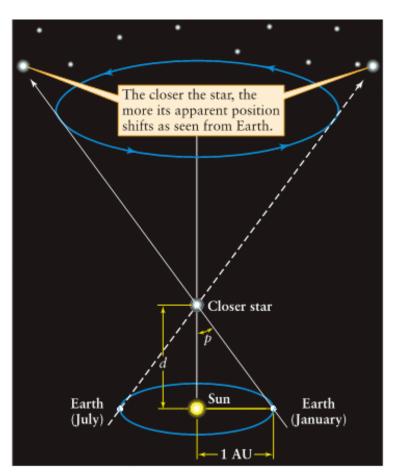
Measuring Distances



Parallax



(a) Parallax of a nearby star



(b) Parallax of an even closer star

The distance d to the star (in parsecs) is just 1 over the parallax angle p (in arcseconds): $\mathbf{d} = \mathbf{1/p}$.

Parallax and Distance

$$p = parallax angle$$

$$d$$
 (in parsecs) = $\frac{1}{p$ (in arcseconds)

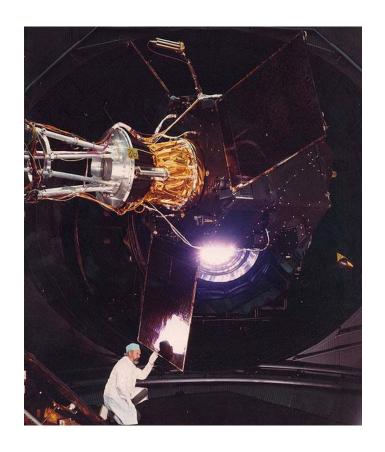
d (in light-years) =
$$3.26 \times \frac{1}{p \text{ (in arcseconds)}}$$

HIPPARCOS

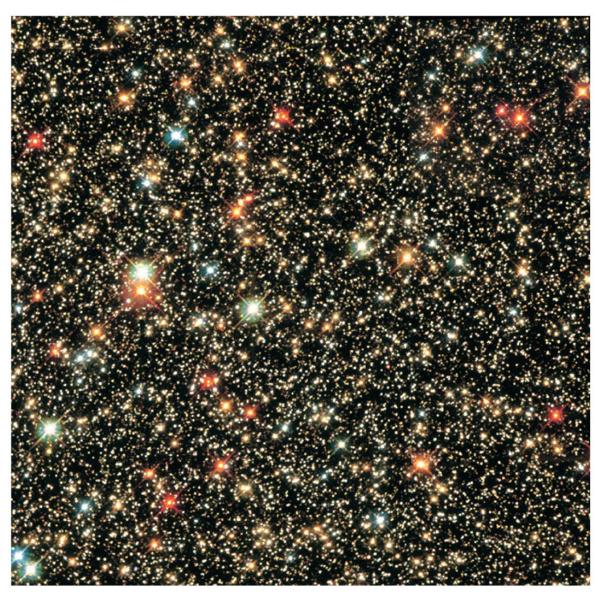
The smallest parallax angle that can be measured from the ground is about 0.01 arcsec so the furthest stars that can have distances measured from the ground are at d = 1/0.01 = 100 pc.

Observations made in space permit measurements of even smaller parallax angles down to 0.001 arcsec corresponding to distances of 1000 pc.

The satellite **Hipparcos** has measured about 118,000 stars using the parallax method.



Hipparcos



 Most luminous stars (not common):

 $10^6 L_{\rm Sun}$

• Least luminous stars (common):

10⁻⁴L_{Sun}

• (*L*_{Sun} is luminosity of Sun)

Magnitude Scale: Apparent Magnitude

The **magnitude scale** is a system used to denote the brightness of an astronomical object.

Keep in mind that the greater the apparent magnitude, the dimmer the star.

A second magnitude star is a factor of 2.512 fainter in brightness than a 1 magnitude star, a third magnitude star is fainter by a factor of 2.512 from a second magnitude star ...

$$m_1 - m_2 = 2.5 \log_{10} \left(\frac{b_2}{b_1} \right)$$

 m_1 , m_2 = apparent magnitudes of sources 1 and 2, respectively b_1 , b_2 = apparant brightnesses of sources 1 and 2, respectively

Magnitude Scale: Apparent Magnitude

$$m_1 - m_2 = 2.5 \log_{10} \left(\frac{b_2}{b_1}\right) \Rightarrow \frac{m_1 - m_2}{2.5} = \log_{10} \left(\frac{b_2}{b_1}\right) \Rightarrow 10^{\frac{m_1 - m_2}{2.5}} = \frac{b_2}{b_1}$$

Example: If the apparent magnitudes of two stars are $m_1 = 15$ and $m_2 = 10$ what is the ratio of the apparent brightnesses of star 2 to star 1 $(b_2/b_1 = ?)$

Solution:

$$\frac{b_2}{b_1} = 10^{\frac{m_1 - m_2}{2.5}} = 10^{\frac{15 - 10}{2.5}} = 10^{\frac{5}{2.5}} = 10^2 = 100$$

Magnitude Scale: Absolute Magnitude

Absolute magnitude: The apparent magnitude that a star would have if it were at a distance of 10 parsecs from Earth.

The apparent magnitude of the Sun is -26.7. If the Sun were moved to a distance of 10 parsecs from the Earth, it would look fainter and have a magnitude of +4.8. (remember larger magnitudes means fainter)

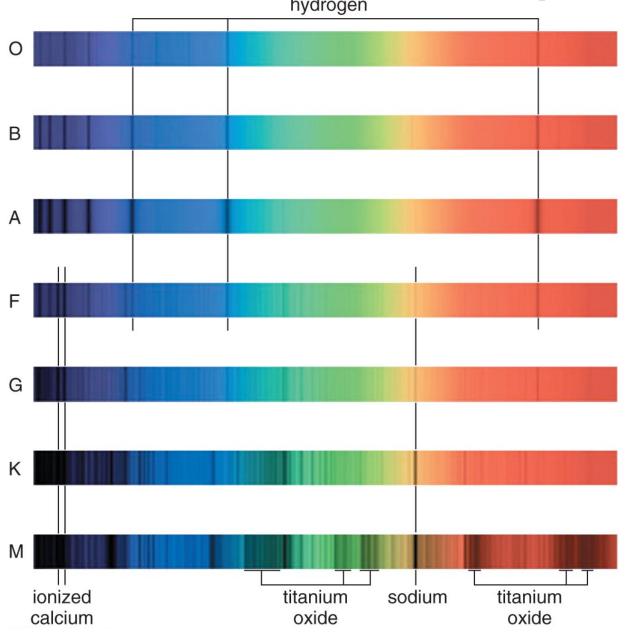
The relation between the apparent and absolute magnitudes of an object is:

$$m - M = 5\log d - 5$$

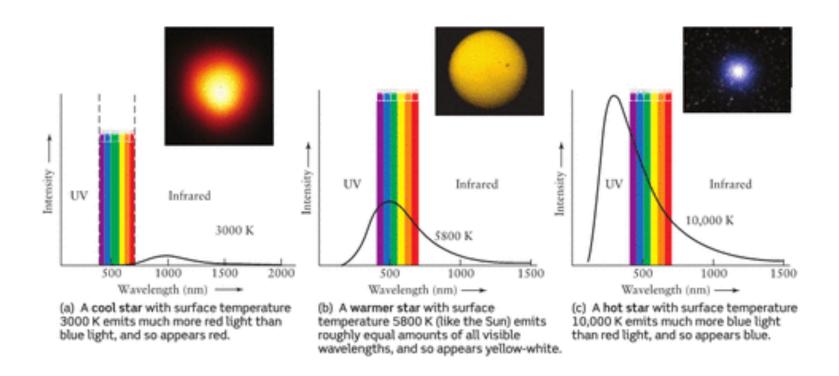
d = distance between the Earth and the object in parsec

m - *M* is referred to as the distance modulus

How do we measure stellar temperatures?

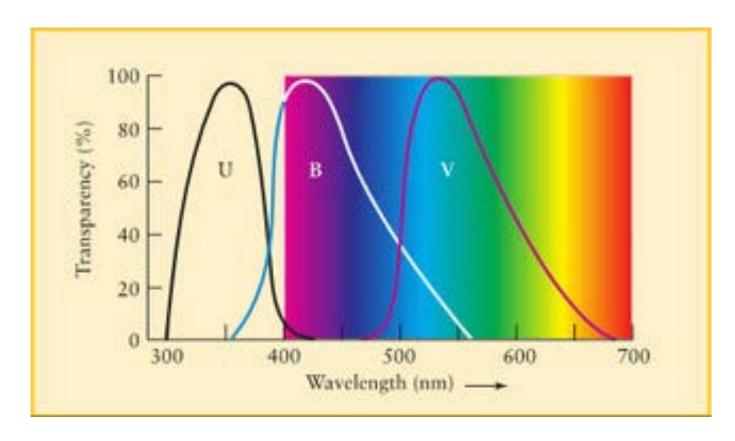


Colors and Temperature



A stars temperature is related its color. Red stars a relatively cold and blue stars are relatively hot.

Measuring Temperatures with Filters



A filter is transparent to a certain wavelength band.

A U filter is more transparent in the ultraviolet band a B filter if more transparent in the blue and a V filter is more transparent in the yellow-green.

Measuring Temperatures with Filters

Method: First measure a stars brightness through each of the U, B and V filters. This gives the apparent brightnesses of b_U , b_B and b_V .

Then compare the relative brightnesses by taking the ratios b_V/b_B and b_B/b_U . These ratios indicate the temperature of the stars surface.

Spectra of Stars

Absorption spectra in stars are produced in the following way:

A star produces a **continuum spectrum** from hot (T_{gas}) dense gas in its atmosphere. This spectrum is very close to that of a **blackbody spectrum** with a temperature of T_{gas} .

The stars continuum radiation goes through cooler parts of its upper atmosphere where **photons of only certain wavelengths** are absorbed.

The wavelengths of the absorption lines are characteristic of the elements and the ionization level of the stars absorbing gas.

Stellar Classification

To bring some order in the zoo of stellar spectra astronomers have grouped stars according to the appearance of their spectra. These classifications of stars according to the appearance of their spectra are called spectral classes.

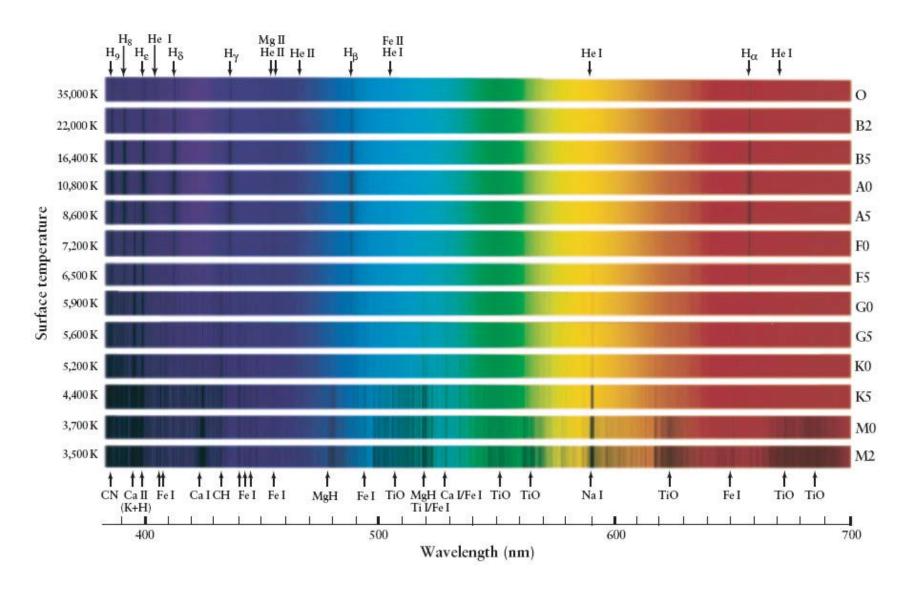
The spectra classes are labeled: OBAFGKMLT

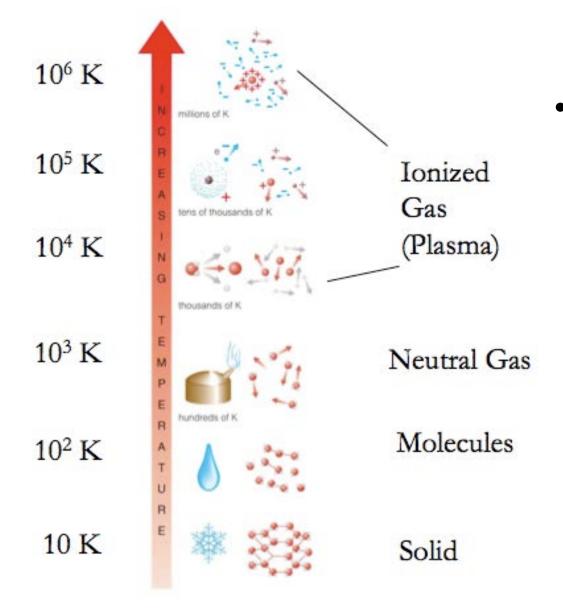
A refined scheme adds a number ranging from 0 to 9 to each letter. This subdivision of the spectral class is called **spectral type**.



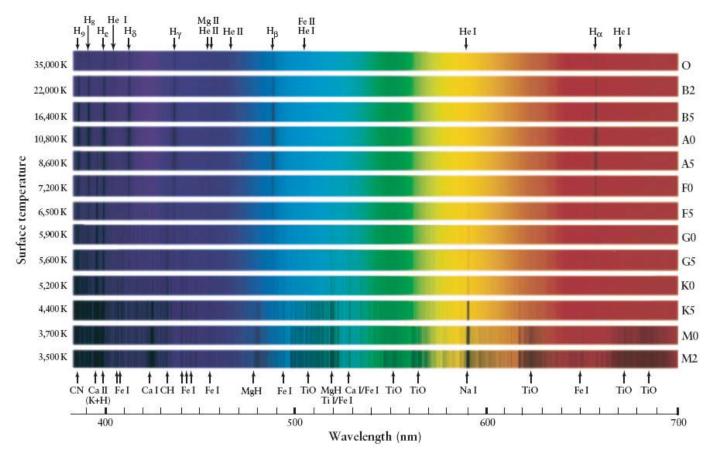
In the late 1800's a team of women at the Harvard College Observatory undertook the task of classifying the spectra of hundreds of thousands of stellar spectra.

Stellar Spectra and Temperature

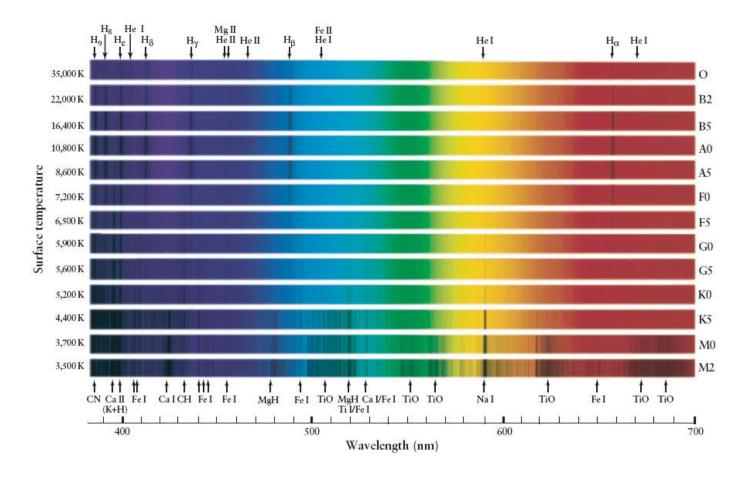




 Level of ionization also reveals a star's temperature.



- Absorption lines in star's spectrum tell us its ionization level and its temperature.
- (Hottest) O B A F G K M (Coolest)



For T > 20,000 K most H atoms are ionized so the Balmer lines are very weak in very hot stars.

For T < 4,000 K most H atoms have electrons in the n = 1 level and the Balmer lines are very weak in very cool stars.

Remembering Spectral Types

(Hottest) O B A F G K M (Coolest)

- Oh, Be A Fine Girl, Kiss Me
- Only Boys Accepting Feminism Get Kissed Meaningfully

Thought Question

Which kind of star is hottest?

- A. M star
- B. F star
- C. A star
- D. K star

Thought Question

Which kind of star is hottest?

- A. M star
- B. F star
- C. A star
- D. K star

Brown Dwarfs

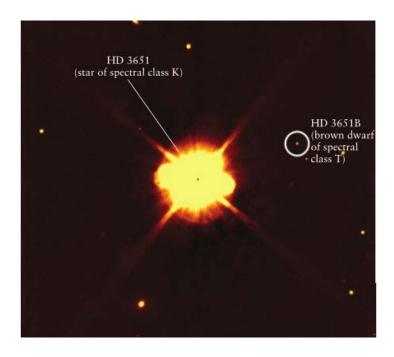
Brown Dwarfs are starlike objects that are not massive enough $(M<0.08 M_{\odot})$ to sustain hydrogen fusion in their core.

They have temperatures lower than those of spectral class M stars.

They are primary heated by Kelvin-Helmoltz contraction.

Since they are so cool their spectra peak in the infrared.

Brown Dwarf spectra have a rich variety of **absorption lines produced by molecules**.



Infrared image of brown dwarf HD3561B. The star HD 3561 is of spectral class K, with a surface temperature of about 5200 K. HD 3651 is orbited by a brown dwarf with a surface temperature between 800 and 900 K and a luminosity just 1/300,000 that of the Sun.

Stellar Radii

Stefan - Boltzmann Law : $F = \sigma T^4$

Inverse Square Law :
$$F = \frac{L}{4\pi R^2}$$

F = flux at the stars surface in W m⁻²

L = stars luminosity in W

R = radius of stars emitting surface in meters

T = temperature of stars surface in kelvins

 σ = Stefan - Boltzmann contant = 5.67 × 10⁻⁸ W m⁻² K⁻⁴

Stellar Radii

$$L = 4\pi R^2 \sigma T^4$$
 Equation (1)

$$L_{\odot} = 4\pi R_{\odot}^2 \sigma T_{\odot}^4$$
 Equation (2)

Dividing equation 1 by equation 2 we have:

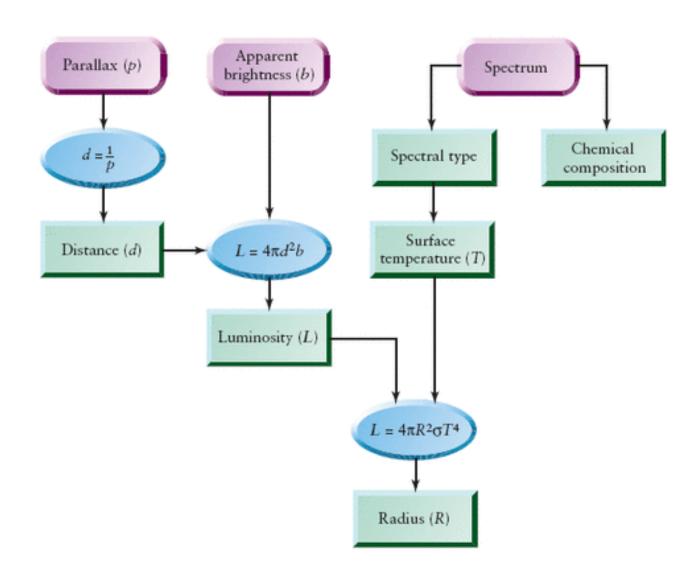
$$L/L_{\odot} = (R/R_{\odot})^2 (T/T_{\odot})^4$$
 Equation (3)

Solving for R/R_{\odot} we have:

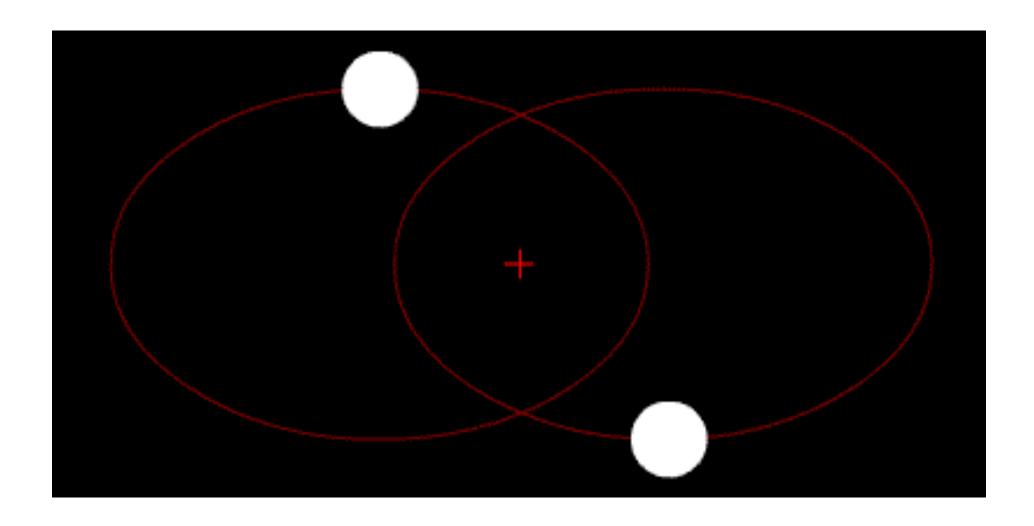
$$R/R_{\odot} = \sqrt{L/L_{\odot}}(T_{\odot}/T)^2$$

Example: The bright reddish star Betelgeuse in the constellation Orion is 60,000 times more luminous than the Sun and has a surface temperature of 3500 K. How much larger is Betelgeuse's radius from the Sun's radius? $(T_{\odot}=5,800 \text{ K})$

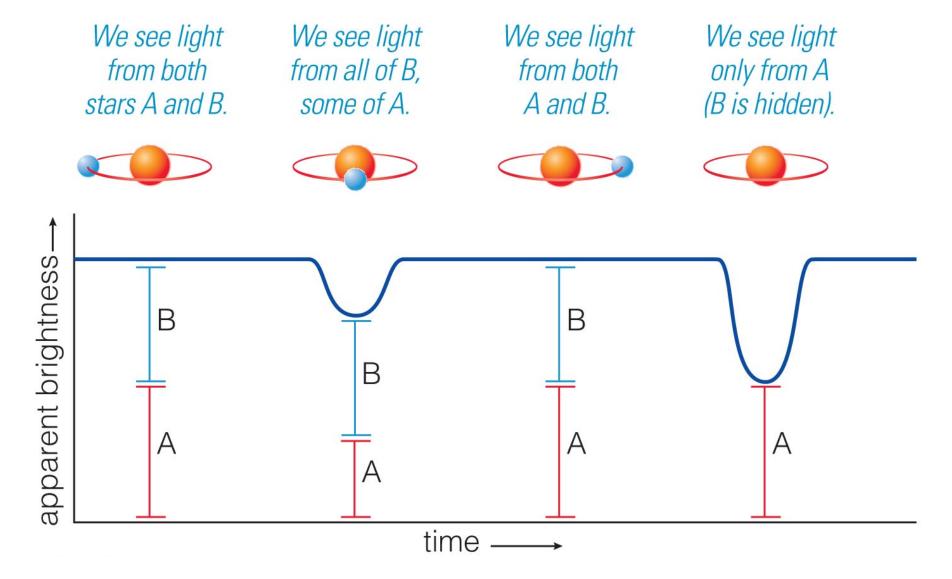
Measuring the Properties of Stars

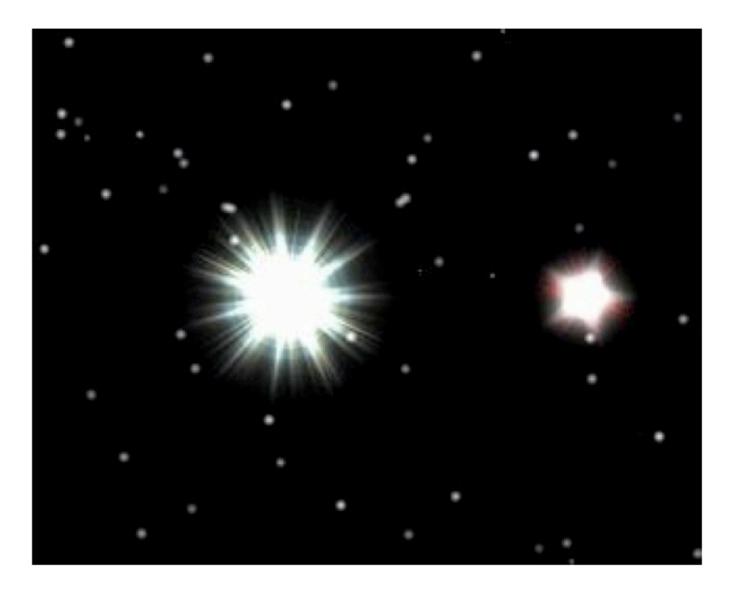


Binary Star Systems



How do we measure stellar masses?





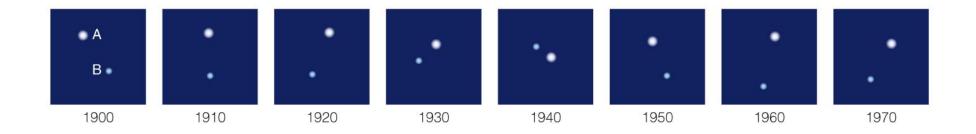
 The orbit of a binary star system depends on strength of gravity.

Types of Binary Star Systems

- Visual binary
- Spectroscopic binary
- Eclipsing binary

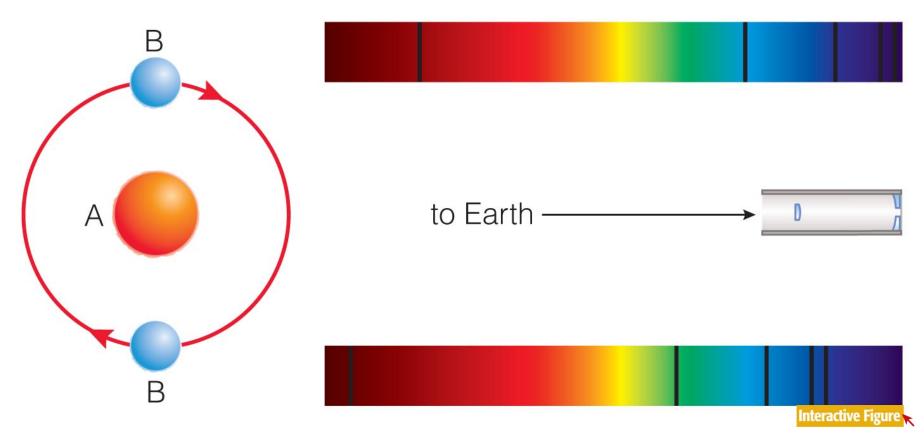
About half of all stars are in binary systems.

Visual Binary



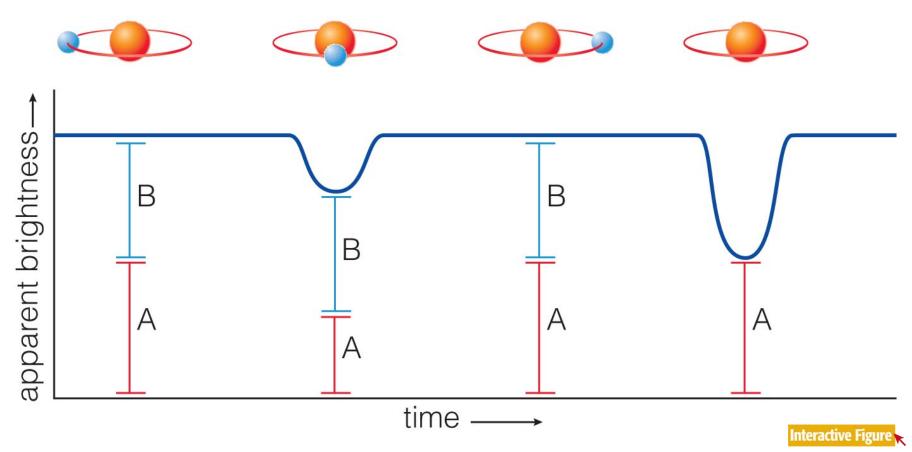
 We can directly observe the orbital motions of these stars.

Spectroscopic Binary



 We determine the orbit by measuring Doppler shifts.

Eclipsing Binary

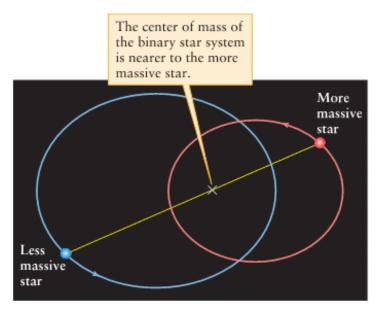


• We can measure periodic eclipses.

Masses of Stars in Binary Systems

$$M_1 + M_2 = \frac{4\pi^2}{G} \frac{a^3}{P^2}$$

$$\frac{M_1}{M_2} = \frac{\mathbf{v}_2}{\mathbf{v}_1} = \frac{a_2}{a_1}$$



(b) A binary star system

P = period of orbit

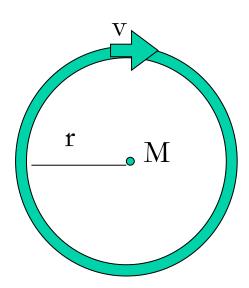
 $a = a_1 + a_2$ (a_1, a_2 are the semimajor axes of the orbits of M_1, M_2 , respectively)

 M_1 , M_2 = masses of stars v_1 , v_2 = orbital velocities of stars

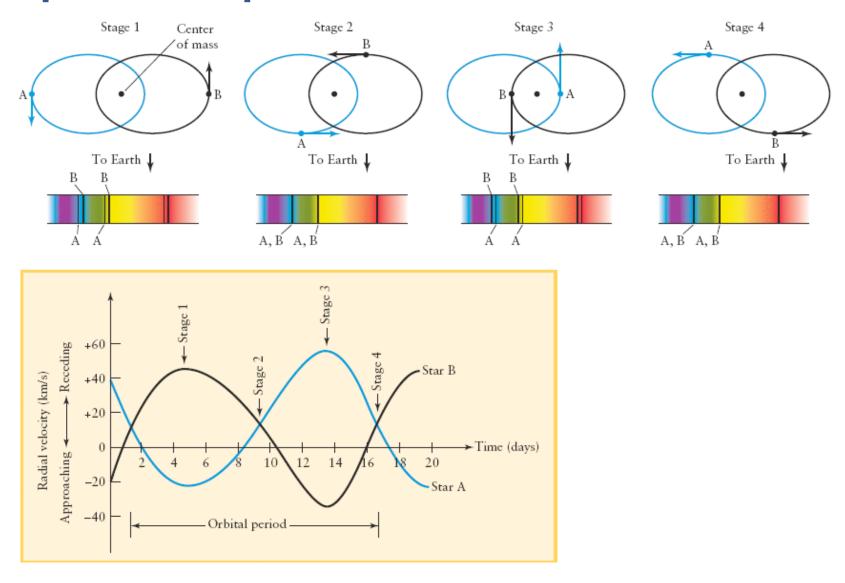
Need two out of three observables to measure mass:

- 1. Orbital period (p)
- 2. Orbital separation (a or r = radius)
- 3. Orbital velocity (v)

For circular orbits, $v = 2\pi r/p$.



Spectroscopic Binaries



Radial Velocity Curves of Spectroscopic binary system HD 171978

What have we learned?

How do we measure stellar luminosities?

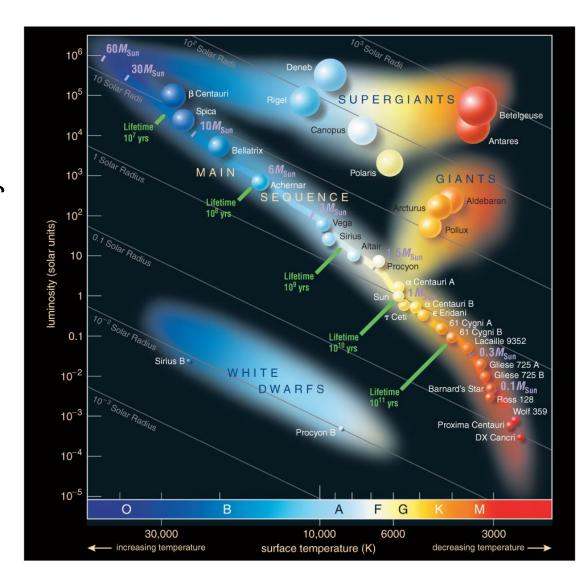
- If we measure a star's apparent brightness and distance, we can compute its luminosity with the inverse square law for light.
- Parallax tells us distances to the nearest stars.
- How do we measure stellar temperatures?
 - A star's color and spectral type both reflect its temperature.

What have we learned?

- How do we measure stellar masses?
 - Newton's version of Kepler's third law tells us the total mass of a binary system, if we can measure the orbital period (p) and average orbital separation of the system (a).

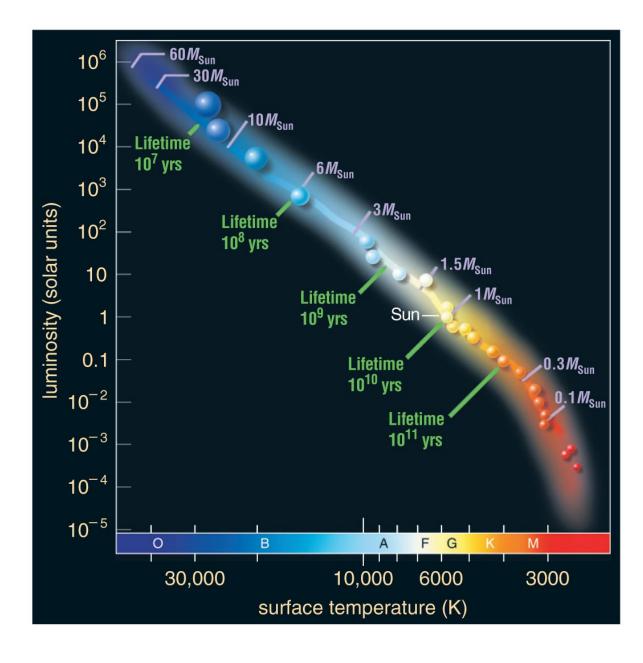
15.2 Patterns Among Stars

- Our goals for learning:
 - What is a Hertzsprung-Russell diagram?
 - What is the significance of the main sequence?
 - What are giants, supergiants, and white dwarfs?
 - Why do the properties of some stars vary?

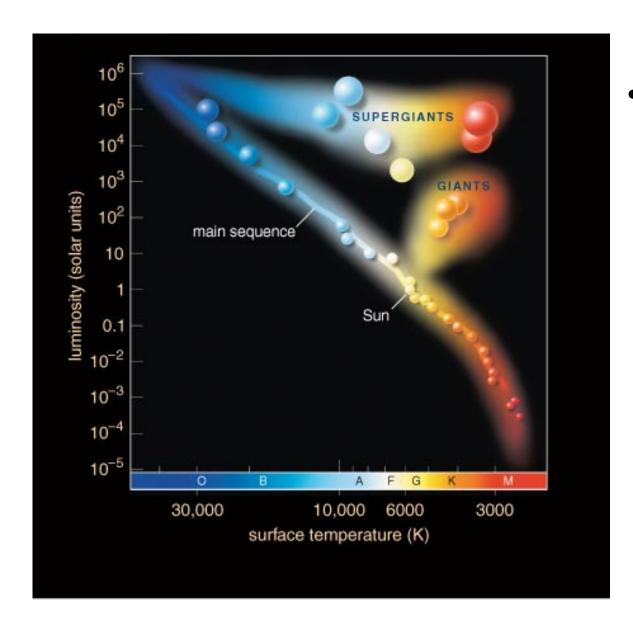


An H-R
 diagram plots
 the luminosity
 and
 temperature of
 stars.

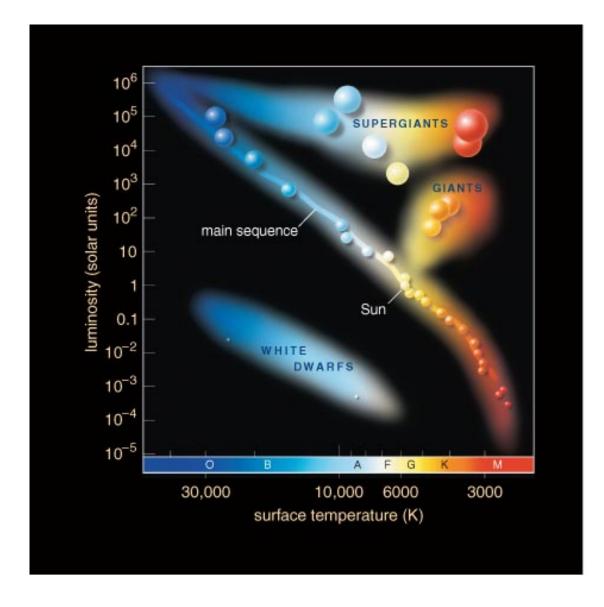




Most stars fall somewhere on the *main* sequence of the H-R diagram.



 Stars with lower T and higher L than main-sequence stars have larger radii. These stars are called *giants* and supergiants.



Stars with higher
 T and lower L
 than main sequence stars
 have smaller
 radii. These
 stars are called
 white dwarfs.

Categories of Stars

Main-sequence stars: hydrogen fusion is taking place in their cores. About 90% of the stars (including the Sun) in the night sky lie along the main sequence.

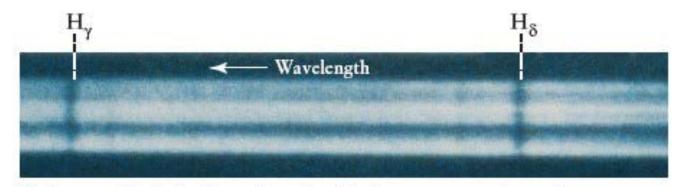
Giant stars: luminosities of 100–1000 L_{\odot} and temperatures of 3000–6000 K. Red giants have T : 3000–5000 K.

Supergiant stars: considerably bigger and brighter than typical red giants, with radii of up to $1000 R_{\odot}$.

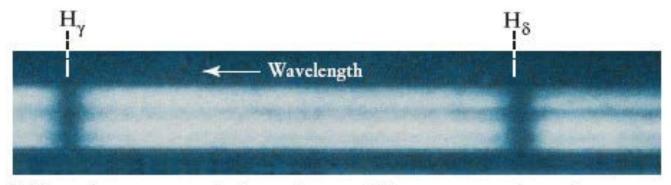
White Dwarfs: A low-mass star that has exhausted all its thermonuclear fuel and contracted to a size roughly equal to the size of the Earth (*has-been star*).

Brown Dwarfs: Starlike (~Jupiter-size, $M < 0.08M_{\odot}$) objects that are not massive enough to sustain hydrogen fusion in their core (*never-will-be star*).

Absorption Line Widths of Stars



 (a) A supergiant star has a low-density, low-pressure atmosphere: its spectrum has narrow absorption lines



(b) A main-sequence star has a denser, higher-pressure atmosphere: its spectrum has broad absorption lines

Absorption Line Widths of Stars

The widths of the absorption lines in stellar spectra depends on the density and pressure of the gas causing the absorption.

The widths of the absorption lines (especially the H lines) indicate the category (ie. main sequence, giant, supergiant) the star belongs to.

In the 1930s W. W. Morgan and P. C. Keenan of the Yerkes Observatory of the University of Chicago classified stars into **luminosity classes** depending on the widths of their lines.

Luminosity Classes: V (Main sequence), IV (Subgiant), III (Giant), II (Bright giant), Ib(Less luminous supergiant) and Ia(Most Luminous supergiant)

Stellar Luminosity Classes

 A star's full classification includes spectral type (line identities) and luminosity class (line shapes, related to the size of the star):

```
I - supergiant
```

II - bright giant

III - giant

IV - subgiant

V - main sequence

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Examples: Sun - G2 V
```

Sirius - A1 V

Proxima Centauri - M5.5 V

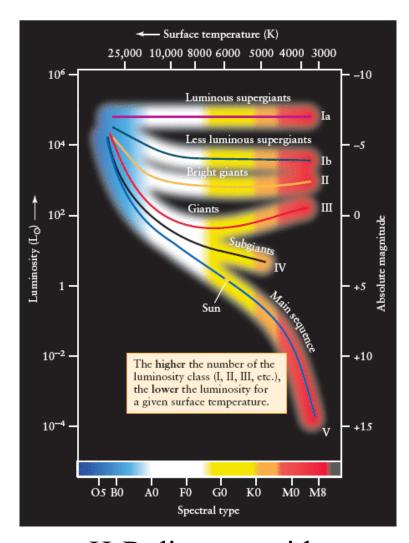
Betelgeuse - M2 I

Stellar Spectral Type and Luminosity Class

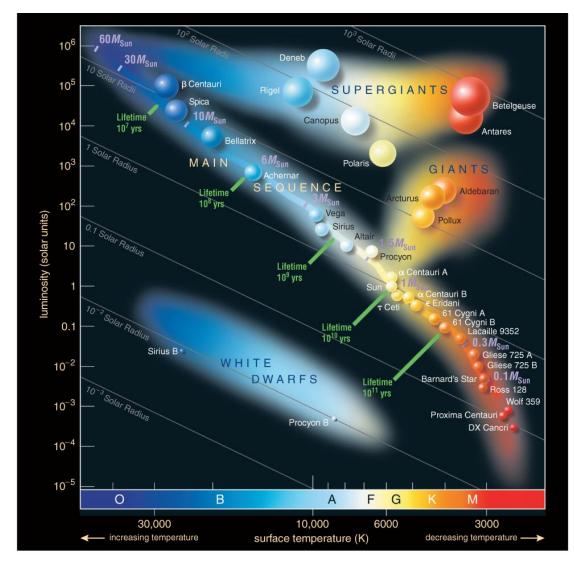
Combining the **spectral type** (which gives the stars temperature) with the **luminosity class** (which indicates on what branch of the H-R diagram the star lies one can estimate the stars luminosity.

Examples: What is the luminosity of

- -a G2 V star?
- -a M0 II star?
- -a B0 Ia star?

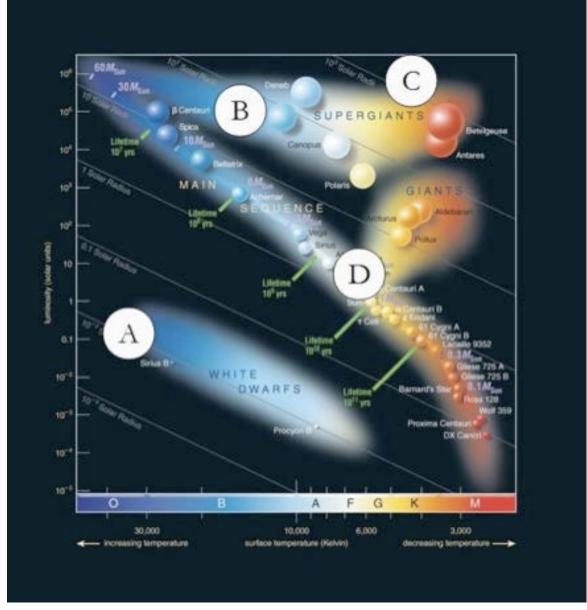


H-R diagram with Luminosity Classes..

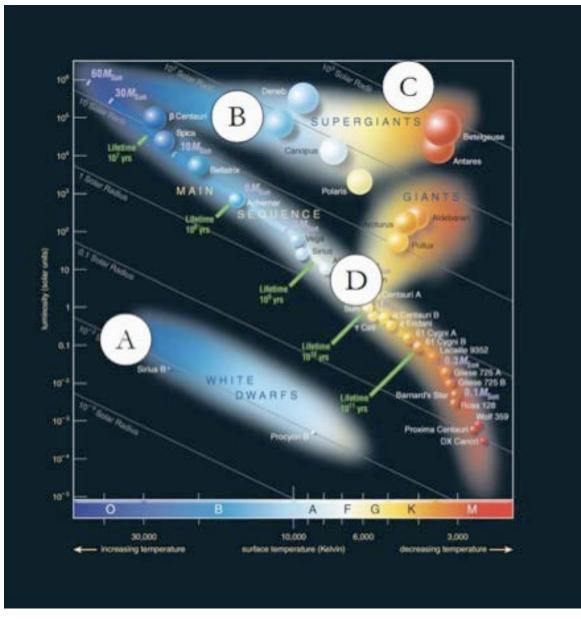


H-R diagram depicts:

Temperature
Luminosity
Luminosity Class
Radius

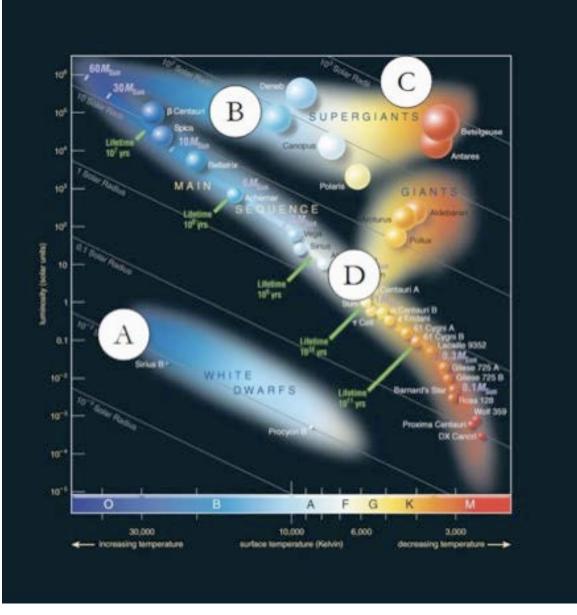


Which star is the hottest?

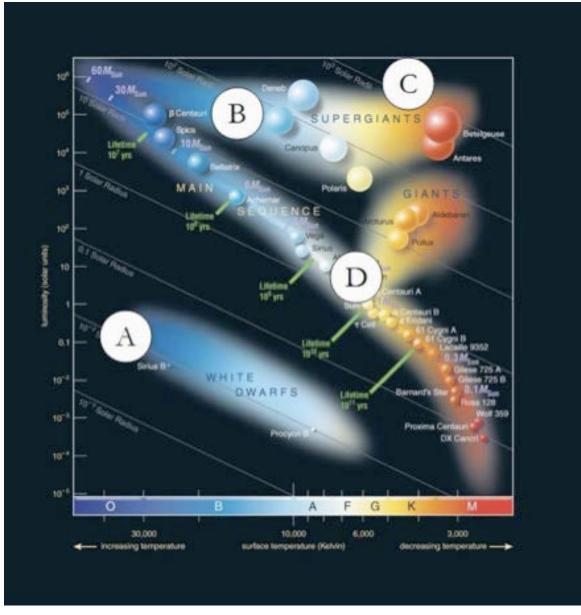


Which star is the hottest?



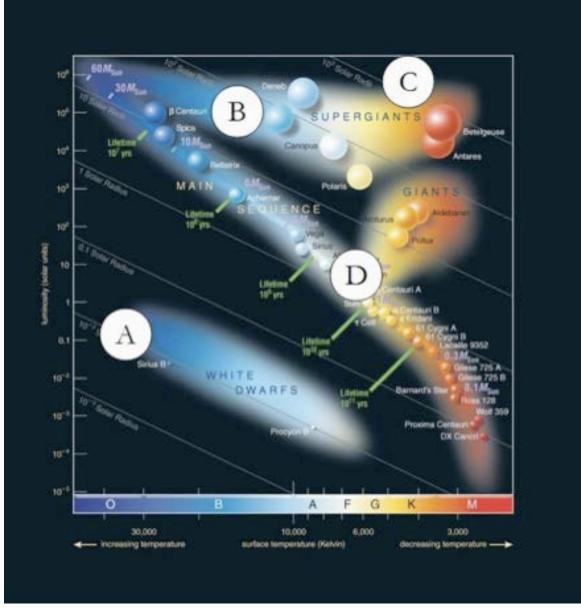


Which star is the most luminous?

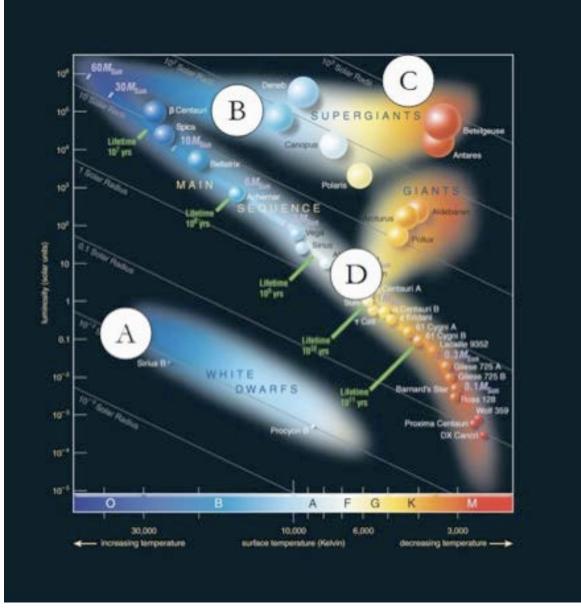


Which star is the most luminous?





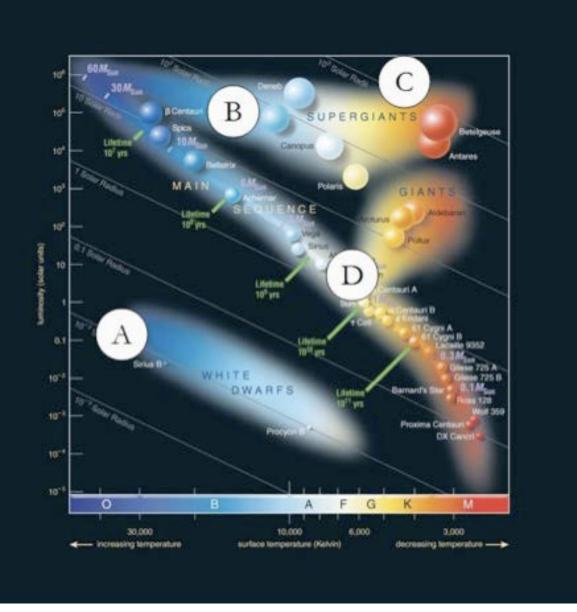
 Which star is a mainsequence star?



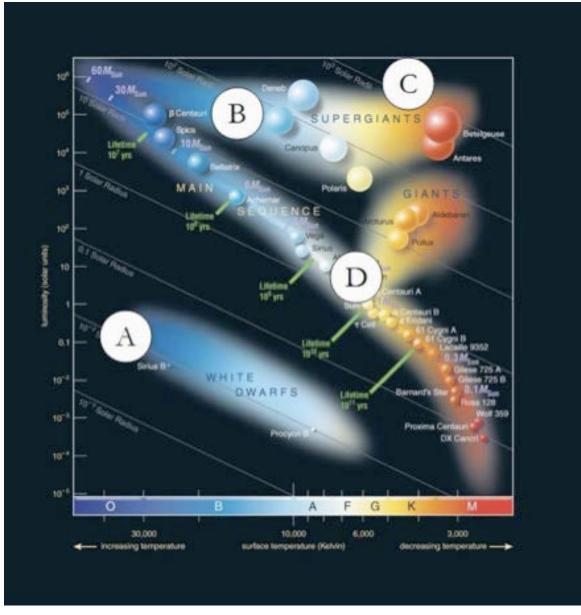
 Which star is a mainsequence star?



Temperature



 Which star has the largest radius?

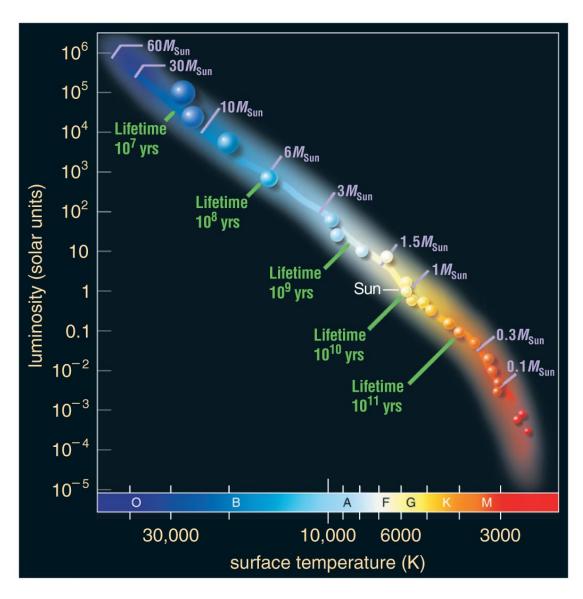


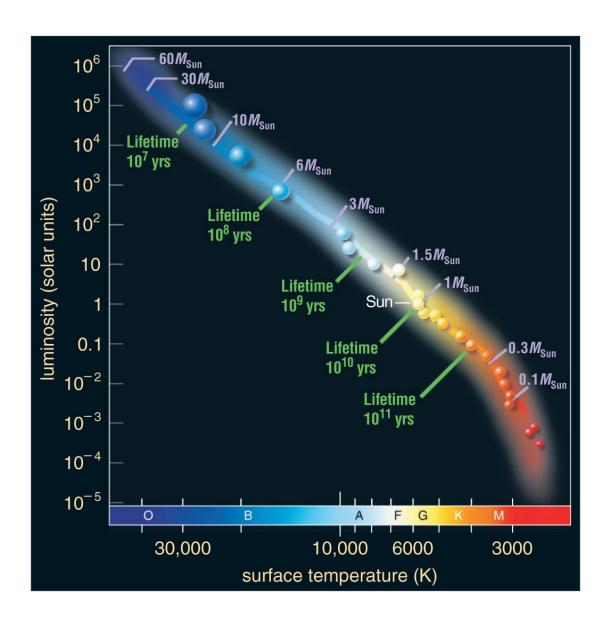
 Which star has the largest radius?

 \bigcirc

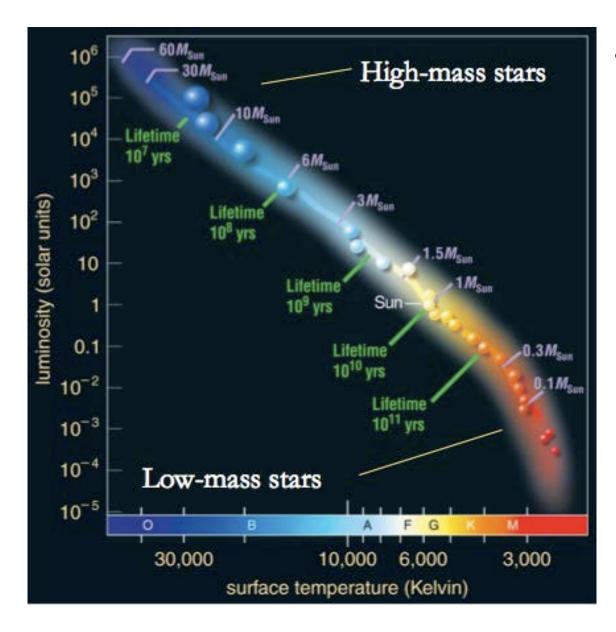
Temperature

What is the significance of the main sequence?

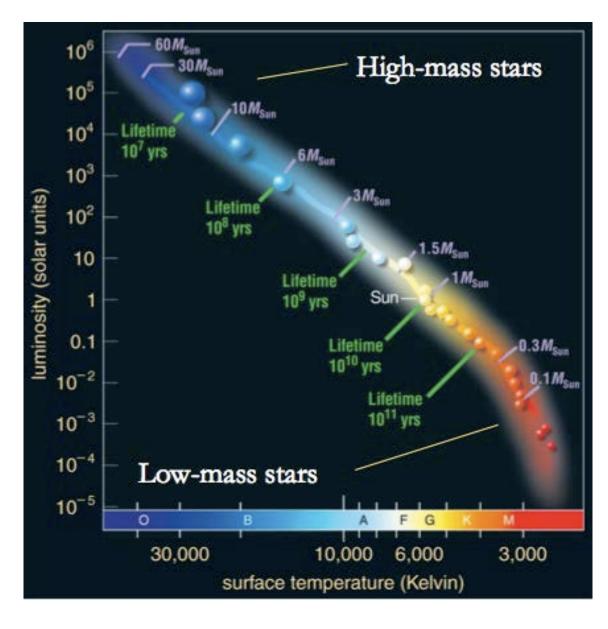




- Main-sequence stars are fusing hydrogen into helium in their cores like the Sun.
- Luminous mainsequence stars are hot (blue).
- Less luminous ones are cooler (yellow or red).



Mass measurements of mainsequence stars show that the hot, blue stars are much more massive than the cool, red ones.

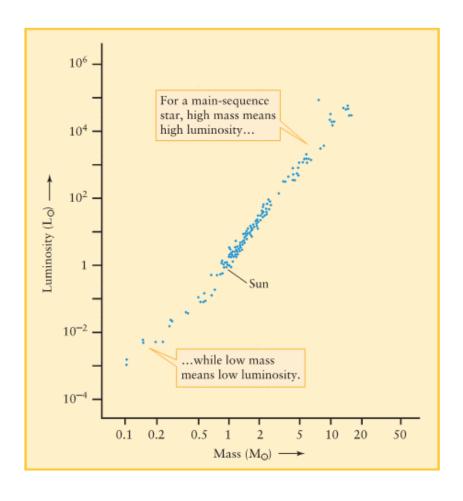


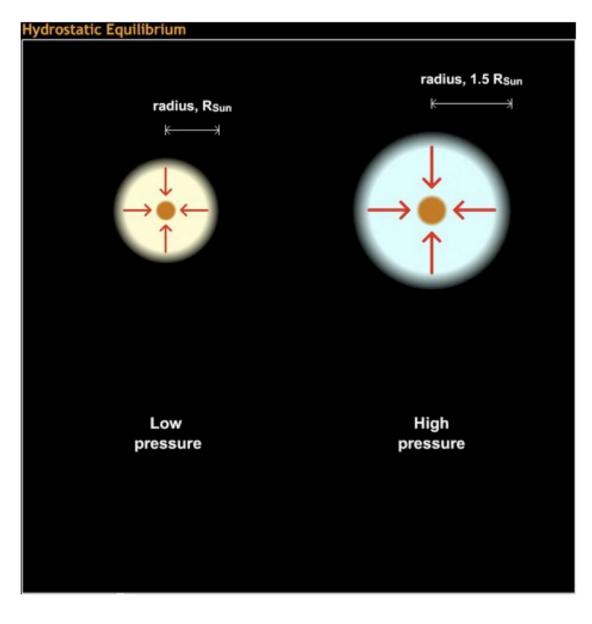
 The mass of a normal, hydrogenburning star determines its luminosity and spectral type.

Mass-Luminosity Relation for Main Sequence Stars

Explaining the M-L correlation:

The more massive a star the larger the pressure, density and temperature in its core in order to balance gravity. This leads to a larger fusion reaction rate and thus a larger luminosity.





- Core pressure and temperature of a higher-mass star need to be larger in order to balance gravity.
- Higher core temperature boosts fusion rate, leading to larger luminosity.

Stellar Properties Review

Luminosity: from brightness and distance

$$(0.08M_{sun})$$
 $10^{-4}L_{sun}-10^{6}L_{sun}$ $(100M_{sun})$

• Temperature: from color and spectral type

$$(0.08M_{sun})$$
 3000 K-50,000 K $(100M_{sun})$

 Mass: from period (p) and average separation (a) of binary star orbit

$$0.08M_{Sun} - 100M_{Sun}$$

Mass and Lifetime

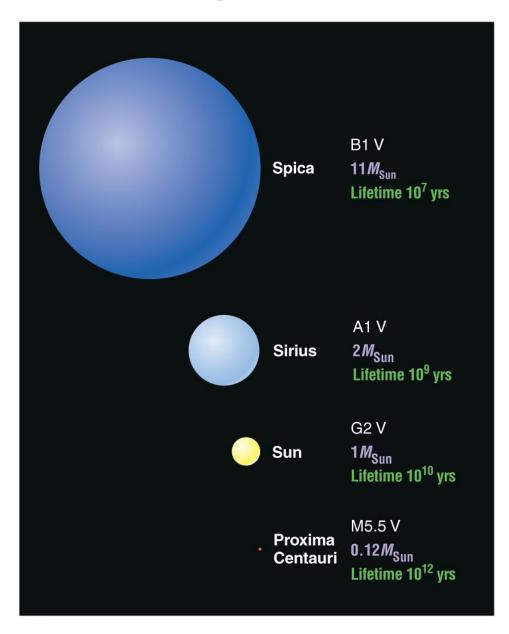
Sun's life expectancy ~ 12 billion years

How long will a star remain on the main sequence? $E = fMc^2$, where f is the fraction of the star's mass that's converted into energy

$$L = \frac{E}{t} \Rightarrow t = \frac{E}{L} = \frac{fMc^2}{L} \propto \frac{M}{M^{3.5}} = \frac{1}{M^{2.5}}$$

$$t_{star} = t_{solar} \left(\frac{M_{solar}}{M_{star}}\right)^{2.5}, t_{solar} = 1.2 \times 10^{10} \text{ years}$$

Main-Sequence Star Summary



High-Mass Star:

- High luminosity
- Short-lived
- Larger radius
- Blue

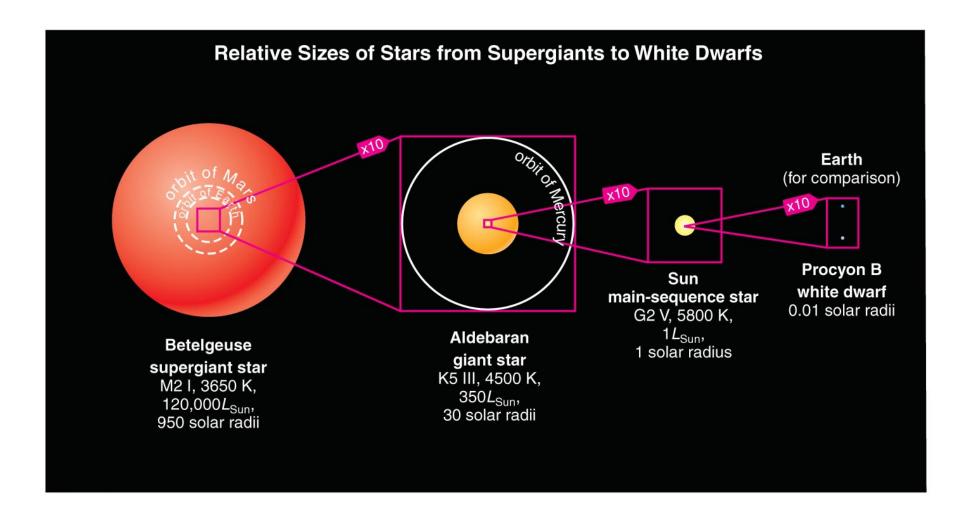
Low-Mass Star:

- Low luminosity
- Long-lived
- Small radius
- Red

What are giants, supergiants, and white dwarfs?

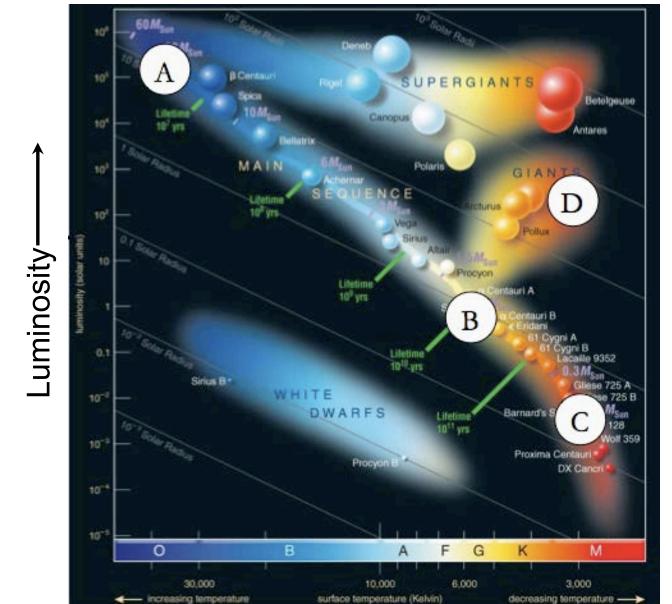


Sizes of Giants and Supergiants



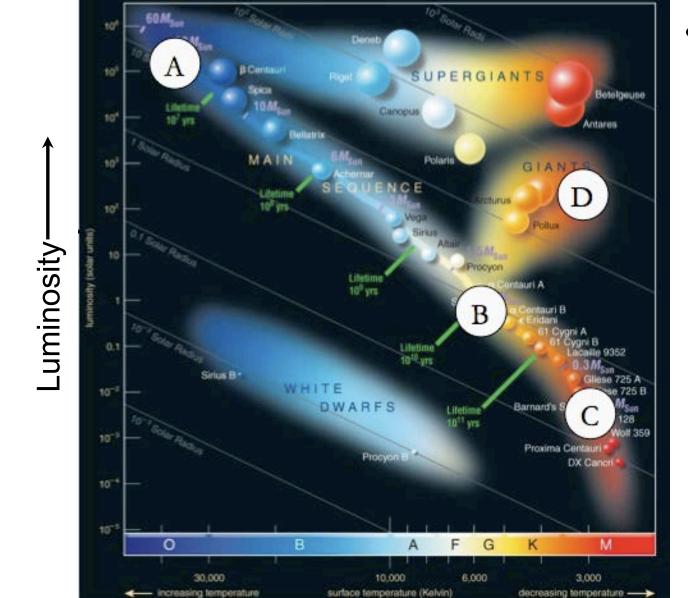
Off the Main Sequence

- Stellar properties depend on both mass and age: Those that have finished fusing H to He in their cores are no longer on the main sequence.
- All stars become larger and redder after exhausting their core hydrogen: giants and supergiants.
- Most stars end up small and white after fusion has ceased: white dwarfs.



 Which star is most like our Sun?

Temperature

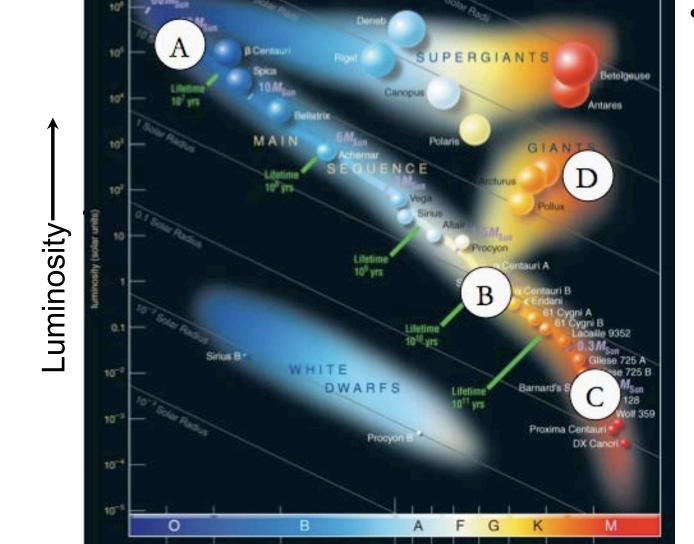


Which star is most like our Sun?

В

Temperature

decreasing temperature -



 Which of these stars will have changed the least 10 billion years from now?

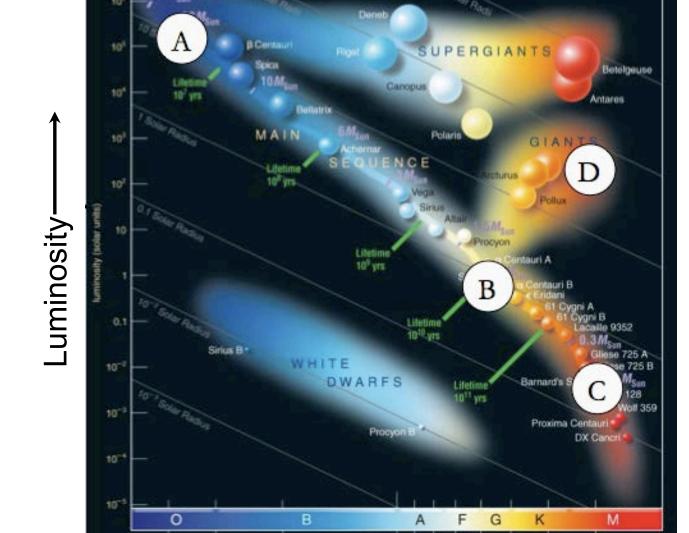
Temperature

surface temperature (Kelvin)

6,000

3,000

30,000



 Which of these stars will have changed the least 10 billion years from now?

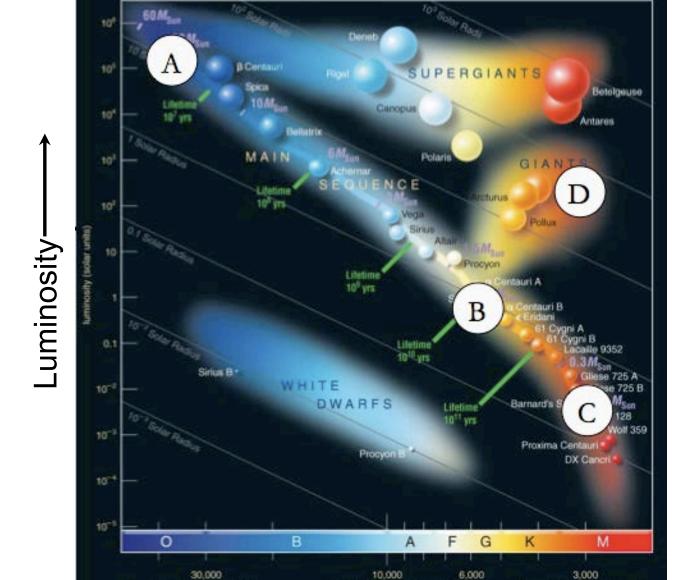
← Temperature

surface temperature (Kelvin)

6,000

3,000

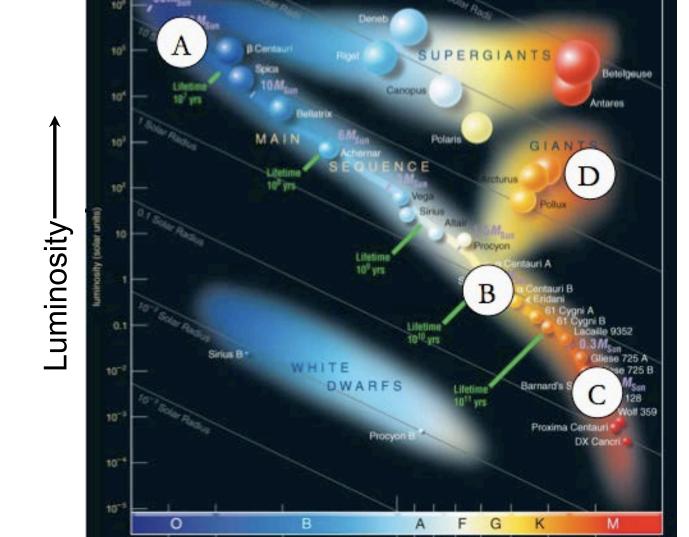
30,000



 Which of these stars can be no more than 10 million years old?

Temperature

surface temperature (Kelvin)



 Which of these stars can be no more than 10 million years old?



Temperature

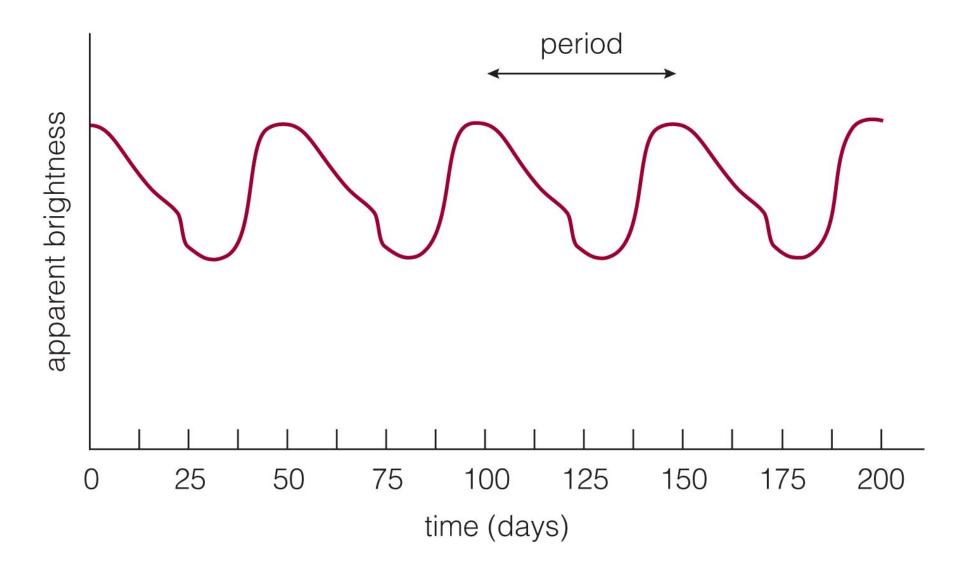
surface temperature (Kelvin)

6,000

3,000

30,000

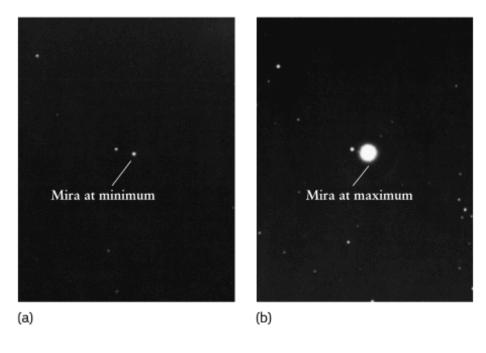
Variable Stars



Variable Stars: Long-Period Variables

Many stars are found to pulsate in size and brightness. These stars are called **pulsating variable stars**.

Long-period variables are pulsating cool red giants that vary in brightness by a factor of 100 over a period of months to years. Typical surface temperatures of long-period variables are ~3,500K and luminosities of 10-10,000 L_{solar}.

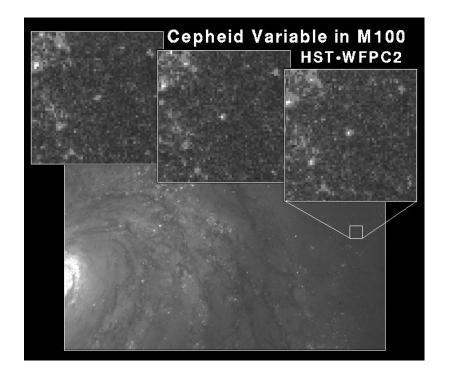


The first **long-period variable** star discovered was Mira (Period ~ 332 days).

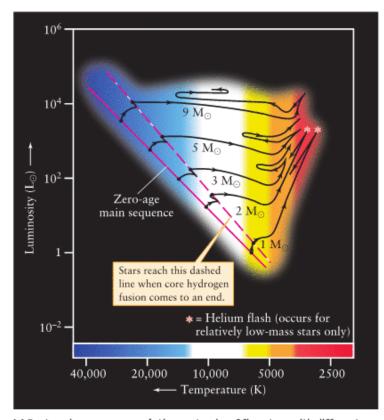
Variable Stars: Cepheid Variables

Pulsating supergiant stars that exhibit rapid brightening followed by gradual dimming with periods ranging from a few to a hundred days are called Cepheid variables.

The first Cepheid variable discovered was δ Cephei.

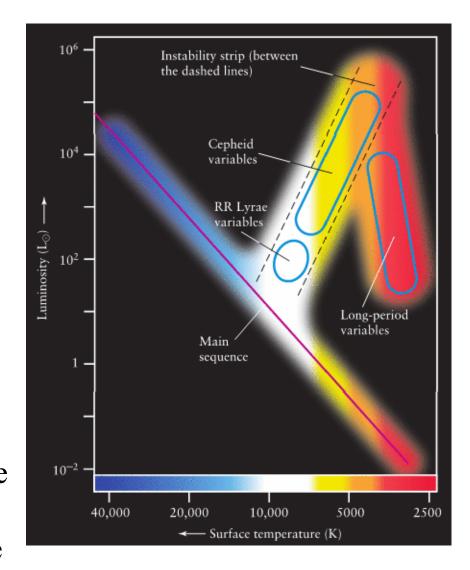


Variable Stars



(a) Post-main-sequence evolutionary tracks of five stars with different mass

After He fusion begins stars move across an instability strip near the middle of the H-R diagram where they begin to pulsate.



Variable Stars

Why Cepheids vary:

When a Cepheid variable pulsates, the star's surface oscillates up and down. During these cyclical expansions and contractions, the star's gases alternately heat up and cool down.

Arthur Eddington suggested that a Cepheid pulsates because the **star is more opaque when compressed** than when expanded. When the star is compressed and opaque, heat cannot easily escape increasing the internal pressure that pushes the star surface outward.

John Cox showed that under certain conditions He in the outer layers of a star becomes ionized and opaque when compressed.

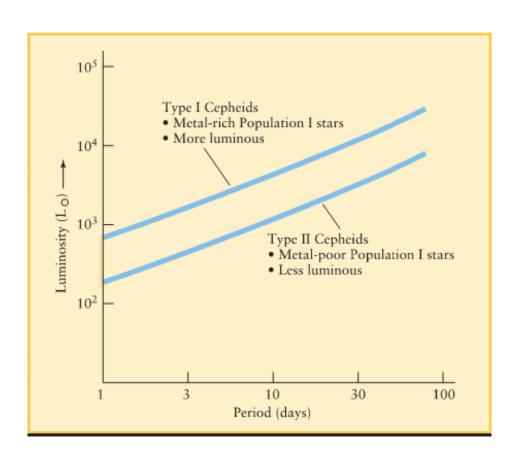
Cepheid Variables: Period-Luminosity Relation

The **P-L relation** together with the brightness of a Cepheid are **used to infer its distance.**

The abundance of metals in a Cepheid's outer layers plays a significant role on how it pulsates.

Metal rich Cepheids are called **Type I Cepheids.**

Metal poor Cepheids are called **Type II Cepheids.**



The period of a Cepheid's pulsations is correlated to its **average luminosity**.

Variable Stars: RR Lyrae Stars

RR Lyrae variables are pulsating horizontal branch stars of spectral class A (and rarely F), with a mass of around half the Sun's. Their periods are less than one day and they are commonly found in globular clusters.

RR Lyrae stars are old, relatively low mass, metal-poor "Population II" stars.

RR Lyrae stars are named for their prototype RR Lyrae in the constellation Lyra.

What have we learned?

What is a Hertzsprung-Russell diagram?

 An H-R diagram plots stellar luminosity of stars versus surface temperature (or color or spectral type).

What is the significance of the main sequence?

- Normal stars that fuse H to He in their cores fall on the main sequence of an H-R diagram.
- A star's mass determines its position along the main sequence (high-mass: luminous and blue; low-mass: faint and red).

What have we learned?

- What are giants, supergiants, and white dwarfs?
 - All stars become larger and redder after core hydrogen burning is exhausted: giants and supergiants.
 - Most stars end up as tiny white dwarfs after fusion has ceased.
- Why do the properties of some stars vary?
 - Some stars fail to achieve balance between power generated in the core and power radiated from the surface.

15.3 Star Clusters

- Our goals for learning:
 - What are the two types of star clusters?
 - How do we measure the age of a star cluster?

What are the two types of star clusters?





Star Clusters

Large cold and dense clouds of gas and dust can collapse to form groups of stars referred to as **star clusters**.

There are two main types of star clusters: open and globular clusters.

Because the stars in a star cluster were all born at roughly the same time, the different **properties of all the stars in a cluster are a function only of mass.** By studying stars clusters we see how stars of different mass evolve differently.

Over time, radiation pressure from the cluster will disperse the molecular cloud. Typically, $\sim 10\%$ of the mass of a gas cloud will coalesce into stars before radiation pressure drives the rest away.

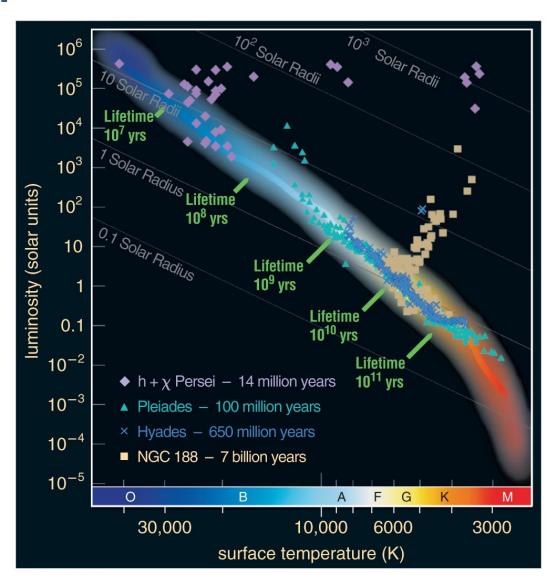


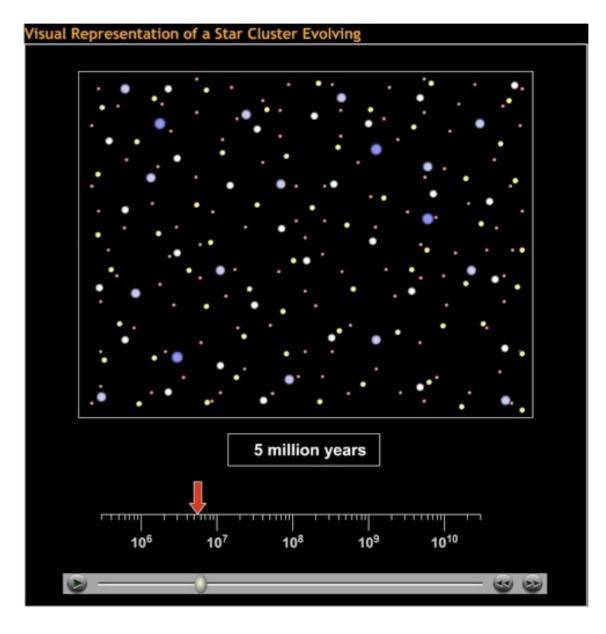
• Open cluster: is a group of up to a few thousand stars that were formed from the same giant molecular cloud, and are still loosely gravitationally bound to each other.



• Globular cluster: Up to a million or more stars in a dense ball tightly bound together by gravity

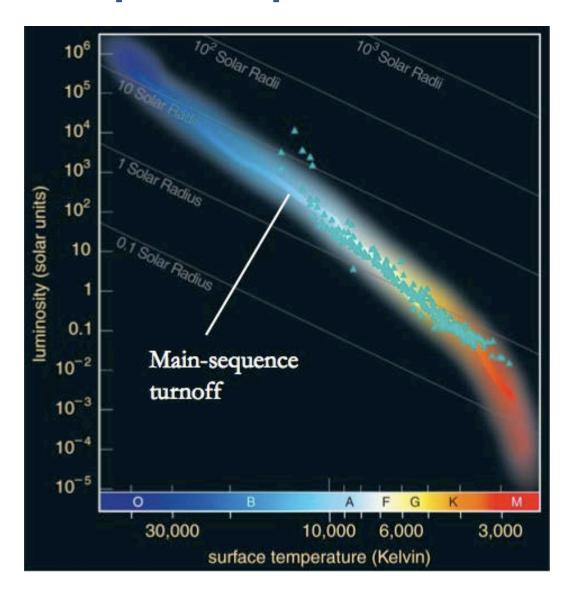
How do we measure the age of a star cluster?





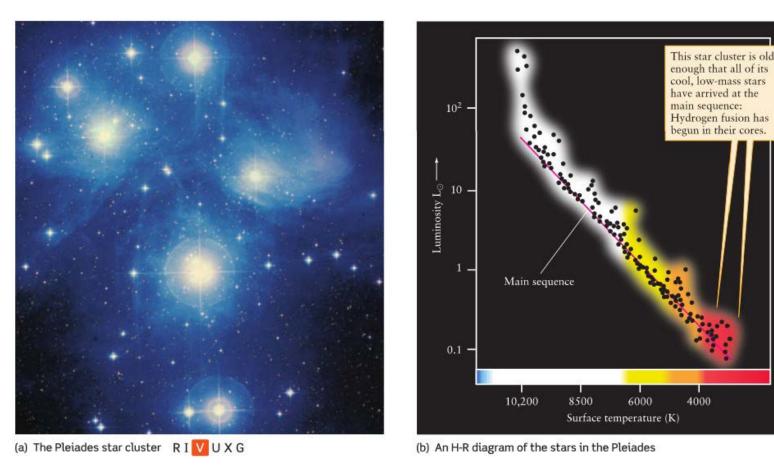
 Massive blue stars die first, followed by white, yellow, orange, and red stars.

Example of Open Cluster: Pleiades

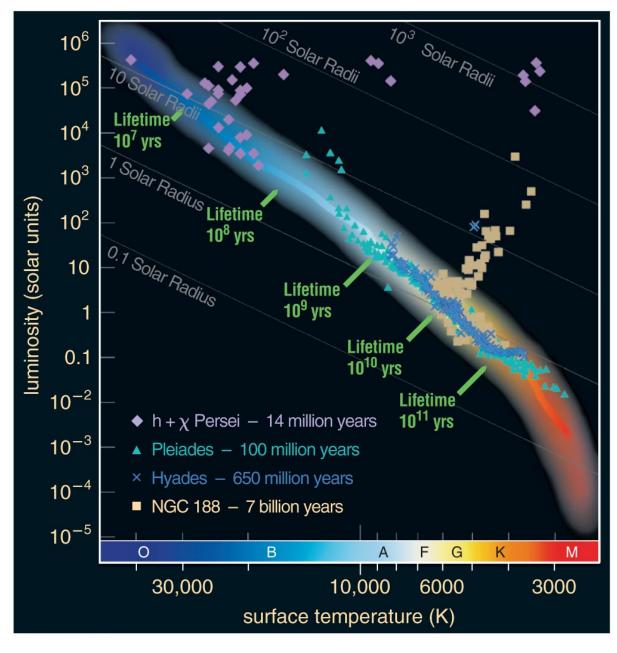


- The Pleiades cluster now has no stars with life expectancy less than around 100 million years.
- Only the most massive stars have left the main sequence

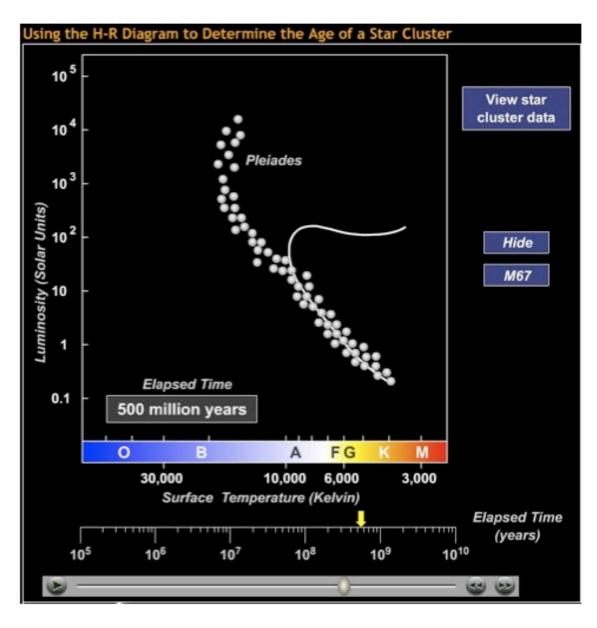
Example of Open Cluster: Pleiades



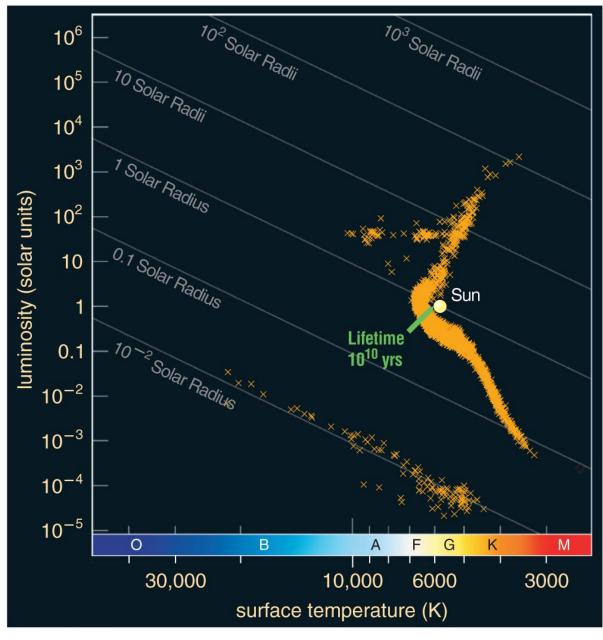
The Pleiades and its H-R Diagram (a) The Pleiades star cluster is 380 ly from Earth in the constellation Taurus. (b) Each dot plotted on this H-R diagram represents a star in the Pleiades. The Pleiades is ~50×10⁶ years old. Notice that the most massive stars have stopped fusing H to He in the core and have moved off the main sequence.



 The mainsequence turnoff point of a cluster tells us its age.



 To determine accurate ages, we compare models of stellar evolution to the cluster data.



Detailed
 modeling of
 the oldest
 globular
 clusters
 reveals that
 they are about
 13 billion
 years old.

What have we learned?

- What are the two types of star clusters?
 - Open clusters are loosely packed and contain up to a few thousand stars.
 - Globular clusters are densely packed and contain hundreds of thousands of stars.
- How do we measure the age of a star cluster?
 - A star cluster's age roughly equals the life expectancy of its most massive stars still on the main sequence.